

Introductory Control Systems

Exercises #15 – Bode Magnitude Diagrams Answers

Note: All frequency ranges given below are **approximate** based on the Bode diagram sketch. The range can be found more accurately and verified using MATLAB®, for example. The estimated range is reasonably accurate in most cases.

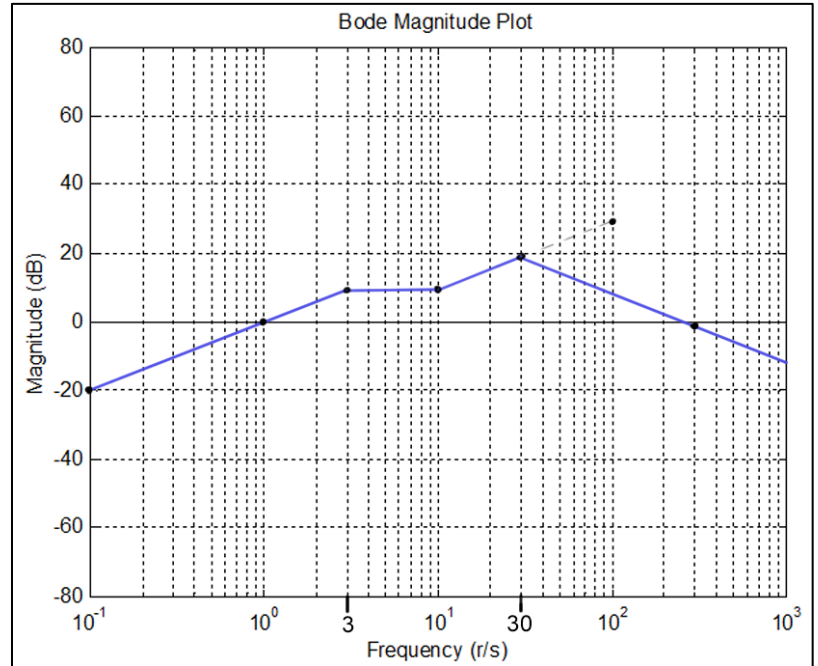
1.
$$G(s) = \frac{270 s(s+10)}{(s+3)(s^2 + 40s + 900)}$$

System amplifies the input ($M > 0$ dB):

$$1 < \omega < 250 \text{ (rad/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega < 1 \text{ (rad/s)} \text{ and } \omega > 250 \text{ (rad/s)}$$



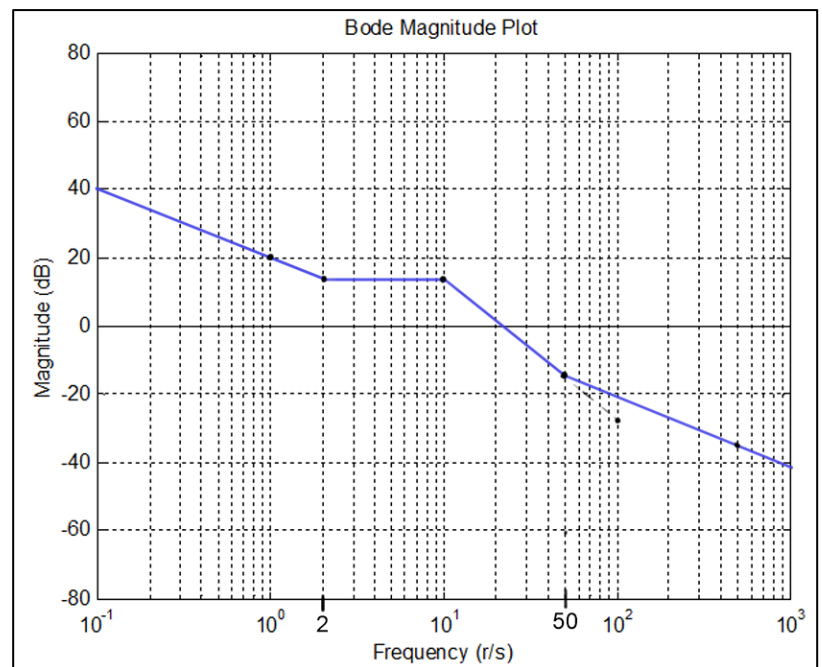
2.
$$G(s) = \frac{10(s+2)(s+50)}{s(s^2 + 15s + 100)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 20 \text{ (rad/sec)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 20 \text{ (rad/s)}$$



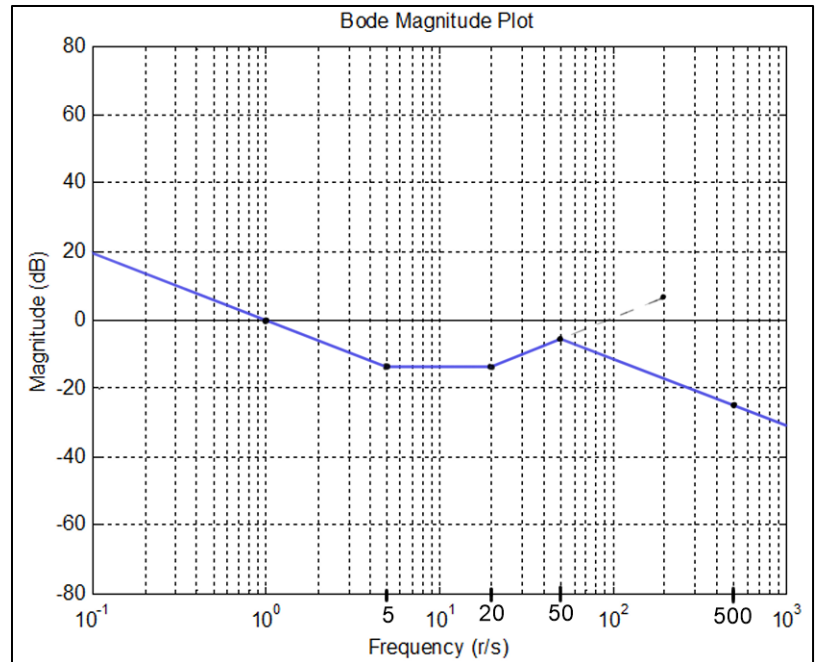
3.
$$G(s) = \frac{25(s+5)(s+20)}{s(s^2 + 70s + 2500)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 1 \text{ (rad/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 1 \text{ (rad/s)}$$



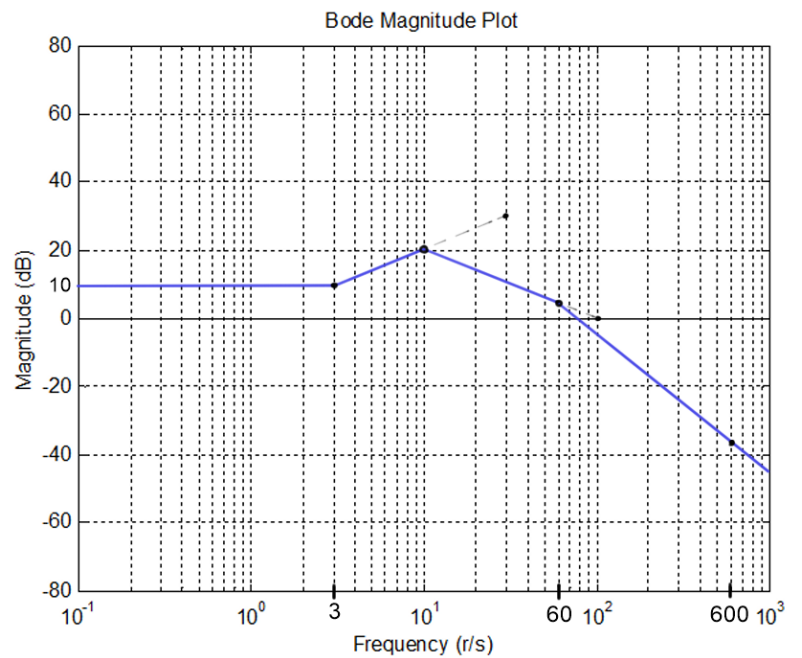
4.
$$G(s) = \frac{6310(s+3)}{(s+60)(s^2 + 15s + 100)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 80 \text{ (rad/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 80 \text{ (rad/s)}$$



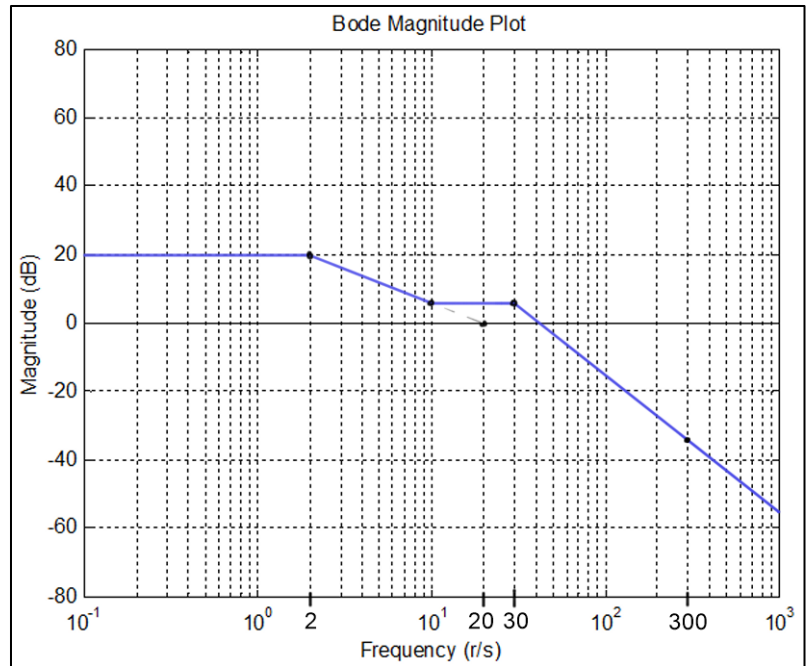
5.
$$G(s) = \frac{1820(s+10)}{(s+2)(s^2+50s+900)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 40 \text{ (rad/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 40 \text{ (rad/s)}$$



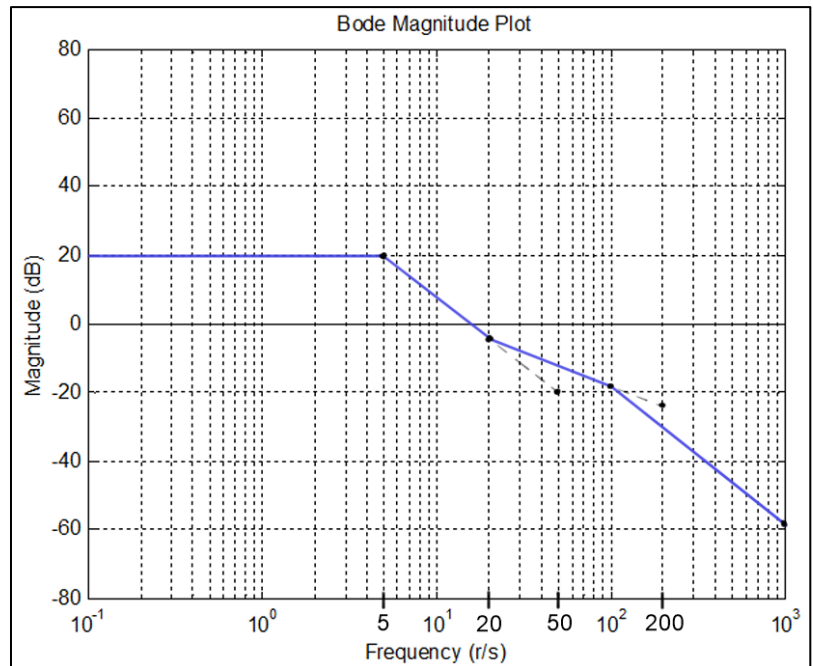
6.
$$G(s) = \frac{1250(s+20)}{(s+100)(s^2+5s+25)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 16 \text{ (rad/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 16 \text{ (rad/s)}$$



7.

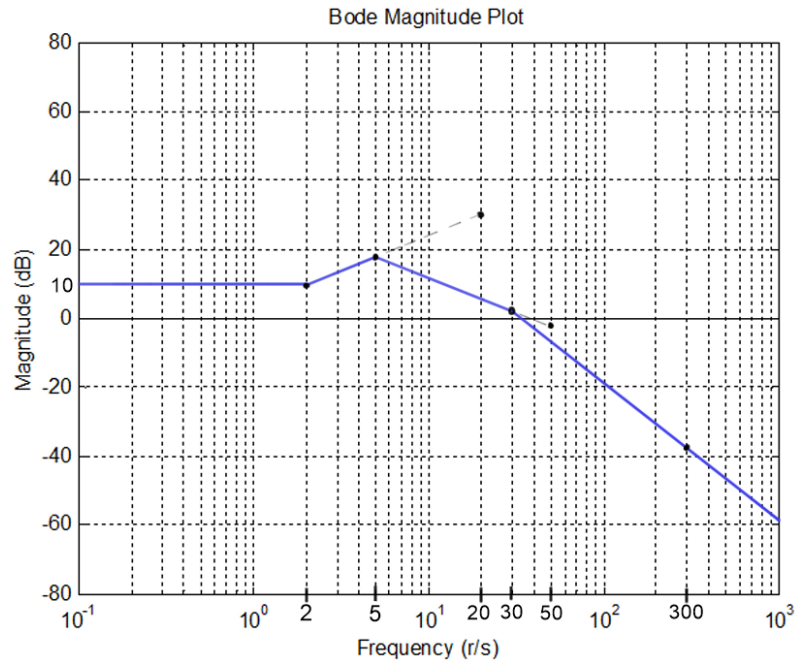
$$G(s) = \frac{1186(s+2)}{(s+30)(s^2+4s+25)}$$

System amplifies the input ($M > 0$ dB):

$$\omega < 32 \text{ (rad/sec)}$$

System attenuates the input ($M < 0$ dB):

$$\omega > 32 \text{ (rad/sec)}$$



8.

$$G(s) = \frac{7906 s}{(s+10)(s^2+70s+2500)}$$

System amplifies the input ($M > 0$ dB):

$$3 < \omega < 85 \text{ (r/s)}$$

System attenuates the input ($M < 0$ dB):

$$\omega < 3 \text{ (rad/s)} \text{ and } \omega > 85 \text{ (rad/s)}$$

