## **Introductory Motion and Control Closed Loop Hydraulic Positioning System**

## Introduction

Fig. 1 shows the **block diagram** of a basic **closed-loop**, **hydraulic actuation system**. The system consists of a **linear proportional control valve**, a **hydraulic cylinder**, and a **proportional controller**. The transfer functions  $G_{v}(s)$  and  $G_{cyl}(s)$  represent the **valve** and **cylinder dynamics**, respectively. The **input** to the system (R(s)) can represent the **desired speed** or **position** of the cylinder, and the **output** (Y(s)) can represent the **actual speed** or **position** of the cylinder.

*Linear proportional valves* are probably better suited for controlling the *velocity* of a hydraulic cylinder because of *dead-band* associated with the valve spool position. However, in the example that follows, a linear proportional valve is used to control the position of a hydraulic cylinder.

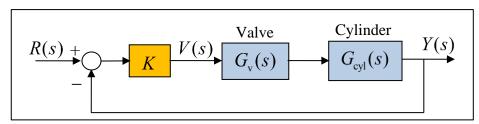


Fig. 1. Block Diagram of a Closed-Loop Hydraulic Actuation System

To understand the response of the closed-loop system, start by analyzing the open loop system shown in Fig. 2. Unfortunately, measurements of this system show the transfer functions  $G_{\rm v}(s)$  and  $G_{\rm cyl}(s)$  both depend on the magnitude of the input voltage V(s). In short, the system is **non-linear**. Analysis of this system is further complicated by **voltage limits** on the valve. The valves, for example, can have an input voltage limit of  $\pm 10$  volts.

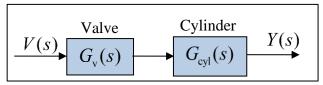


Fig. 2. Block Diagram of an Open-Loop Hydraulic Actuation System

It should be noted that, even though the transfer functions  $G_{\rm v}(s)$  and  $G_{\rm cyl}(s)$  do change as the input voltage V(s) changes, the *form* of the transfer functions *does not change*. In fact, for some range of voltages, the *transfer functions are similar*. For example, transfer functions calculated

for a 5-volt command tend to provide reasonable predictions of the cylinder position response for a 7-volt command.

## Root Locus Analysis of Closed Loop System

To get an initial estimate of what proportional gain K could be used for the closed loop system, the transfer functions derived from the 5-volt data will be used. This should be a good representation of the system at larger voltages. In this case, the loop transfer function is

$$GH(s) = \frac{116303}{s(s+27.864)(s^2+127.83s+10417)}$$
(1)

The *root locus diagram* shown in Fig. 3 indicates the system will be *stable* for 0 < K < 190 and the two slowest poles will be *critically damped* for  $K \approx 15$ .

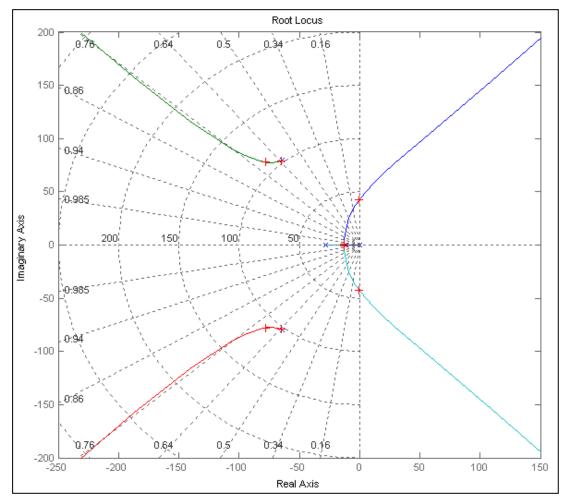


Fig. 3. Root Locus Diagram for Hydraulic Actuation System of Eq. (1)

## Simulation of the Closed Loop System

Fig. 4 shows a *Simulink model* of the closed loop hydraulic actuation system. As in the root locus analysis, the valve and cylinder transfer functions were derived from the 5-volt data. The model assumes these transfer functions apply for all voltages, and in this sense, it is a *linear* model. However, the model also includes the *non-linear* effects of *saturation* and *dead-band*. The *command* to the *valve* and the *valve spool position* are both forced to be in the range of  $\pm 10$  volts (saturation), and for small commands it is assumed to have no response (dead-band).

The code sends the calculated data for *valve command*, *valve response*, *cylinder speed*, and *cylinder position* to the MATLAB workspace for later plotting and analysis.

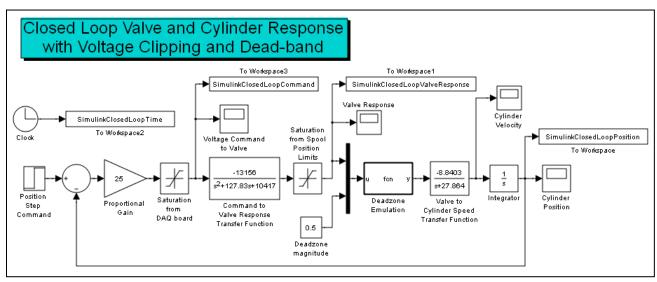


Fig. 4. Simulink Model of Closed Loop Hydraulic Actuation System

Fig. 5 shows the *model* and *test results* using a proportional gain of K = 25, *saturation limits* of  $\pm 10$  volts, and a *dead-band* of  $\pm 0.5$  volts. Note the *valve command* is *saturated* for about the first 1.8 seconds of the run forcing the cylinder to run at *maximum speed* until it is close to the final value. At that point the *valve command* quickly *decreases* to its *minimum value*. Note that when the command gets within the *dead-band*, the cylinder velocity goes to zero. As a result, the final position of the cylinder may exhibit a steady-state error.

The "closed-loop" system behaves like an "open-loop" system for about the first 1.8 seconds of the response. After that time, as the command reduces to its lowest value, the system behaves as a closed-loop system. Because the transfer functions will vary with command magnitude, the actual system will not have this exact response.

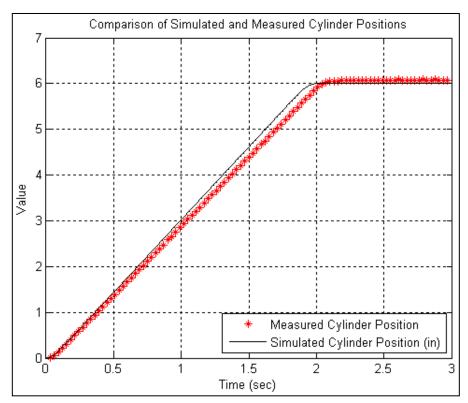


Fig. 5. Closed Loop Cylinder Step Response (6-inch step)

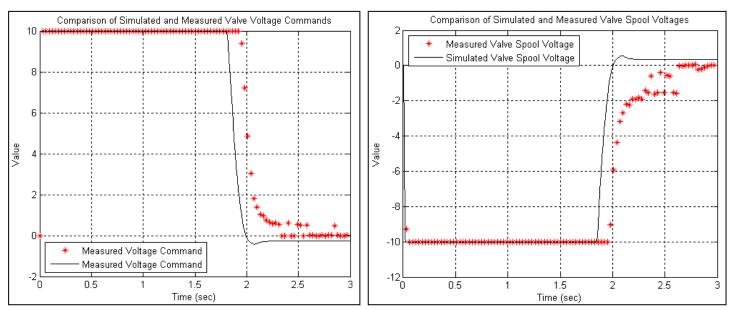


Fig. 6. Closed-loop Valve Command and Spool Responses