

### Elementary Dynamics Example #34: (Rigid Body Kinematics – Instantaneous Centers)

Given:  $R = 3$  (in),  $L = 6$  (in),  $\theta = 30$  (deg)

$$\omega_{OA} = \dot{\theta} = 100 \text{ (rpm) (CCW)}$$

Find:  $\omega_{AB}$ ,  $v_B = \dot{s}$

Solution:

To find the instantaneous center (IC) for the connecting link  $AB$  construct a line perpendicular to the velocity of  $A$ , and construct a second line perpendicular to the velocity of  $B$ . The intersection of these two lines is the IC of  $AB$  and is shown as point  $C$  on the diagram.

Using the triangle  $OAB$ , write

$$R \sin(\theta) = L \sin(\phi)$$

$$\Rightarrow \phi = \sin^{-1} \left( \left( \frac{R}{L} \right) \sin(\theta) \right) = 14.4775 \text{ (deg)}$$

and

$$s = R \cos(\theta) + L \cos(\phi) = 8.40755 \text{ (in)}$$

Using the right-triangle  $OBC$ , write

$$(R + r_A) \cos(\theta) = s \Rightarrow r_A = \left( \frac{s}{\cos(\theta)} \right) - R = 6.7082 \text{ (in)}$$

$$\frac{r_B}{s} = \tan(\theta) \Rightarrow r_B = s \tan(\theta) = 4.8541 \text{ (in)}$$

Velocity Analysis:

$$\left. \begin{aligned} v_A &= R \omega_{OA} = r_A \omega_{AB} \\ \Rightarrow \omega_{AB} &= \left( \frac{R}{r_A} \right) \omega_{OA} = 4.68321 \approx 4.68 \text{ (r/s) (CW)} \end{aligned} \right\} \Rightarrow \omega_{AB} = -4.68 \hat{k} \text{ (r/s)}$$

$$v_B = r_B \omega_{AB} = 22.7328 \approx 22.7 \text{ (in/s) to the left} \quad \underline{v_B \approx -22.7 \hat{i} \text{ (in/s)} \approx -1.89 \hat{i} \text{ (ft/s)}}$$

Note:

As noted in the previous example, the analyst must determine the directions (or signs) of the calculated motions.