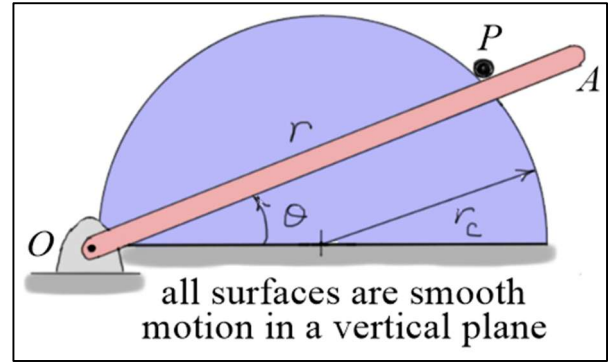


## Elementary Dynamics Example #18: (Newton's Laws, Radial & Transverse Components)

Given:  $W_P = W = 0.5$  (lb), size of  $P$  is negligible  
 $r(\theta) = 2r_C \cos(\theta)$  (ft),  $r_C = 0.4$  (ft)  
 @  $\theta = 30$  (deg),  $\dot{\theta} = 0.4$  (r/s),  $\ddot{\theta} = 0.8$  (r/s<sup>2</sup>)  
 thickness of bar  $OA$  is negligible



Find:  $F_{OA}$  the force bar  $OA$  exerts on  $P$   
 $F_s$  the force the fixed surface exerts on  $P$

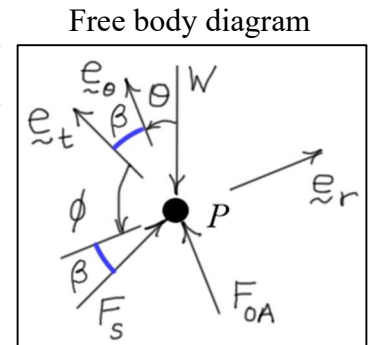
Solution:

Kinematics:

$$r(30) = 2(0.4)\cos(30) \approx 0.69282 \text{ (ft)}, \quad v_\theta = r\dot{\theta} \approx 0.277128 \text{ (ft/s)}$$

$$v_r(30) = (\dot{r})_{\theta=30^\circ} = (-0.8\dot{\theta}\sin(\theta))_{\theta=30^\circ} \approx -0.16 \text{ (ft/s)}$$

$$\phi = \tan^{-1}\left(\frac{v_\theta}{|v_r|}\right) = \tan^{-1}\left(\frac{0.277128}{0.16}\right) = 60 \text{ (deg)} \quad \beta = 90 - \phi = 30 \text{ (deg)}$$



$$(\ddot{r})_{\theta=30^\circ} = \left(\frac{d\dot{r}}{dt}\right)_{\theta=30^\circ} = (-0.8(\ddot{\theta}\sin(\theta) + \dot{\theta}^2\cos(\theta)))_{\theta=30^\circ} \approx -0.430851 \text{ (ft/s}^2\text{)}$$

$$a_r = \ddot{r} - r\dot{\theta}^2 \approx -0.541703 \text{ (ft/s}^2\text{)}, \quad a_\theta = r\ddot{\theta} + 2\dot{r}\dot{\theta} \approx 0.426256 \text{ (ft/s}^2\text{)}$$

Kinetics:

$$\nearrow \sum F_r = F_s \cos(30) - W \sin(\theta) = \left(\frac{W}{g}\right)a_r$$

$$\Rightarrow F_s = \left(W \sin(\theta) + \left(\frac{W}{g}\right)a_r\right) / \cos(30) \approx 0.278962 \approx 0.279 \text{ (lb)}$$

$$\nwarrow \sum F_\theta = F_{OA} + F_s \sin(30) - W \cos(\theta) = \left(\frac{W}{g}\right)a_\theta$$

$$\Rightarrow F_{OA} = -F_s \sin(30) + W \cos(\theta) + \left(\frac{W}{g}\right)a_\theta \approx 0.30015 \approx 0.300 \text{ (lb)}$$