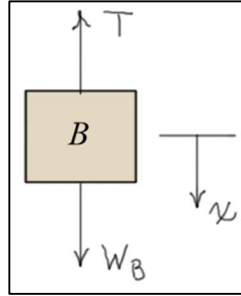
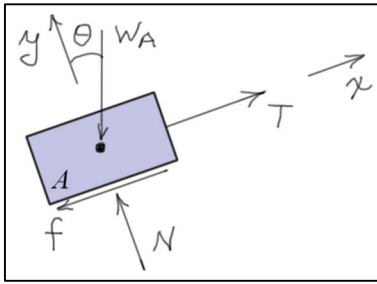
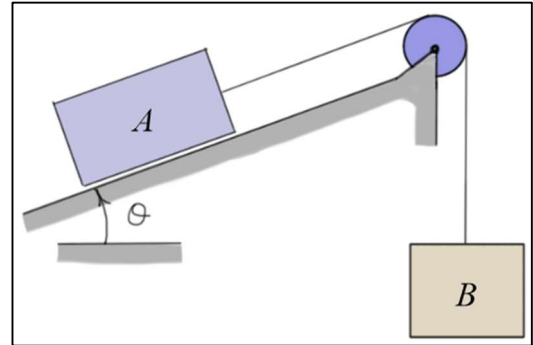


## Elementary Dynamics Example #23: (Impulse & Momentum)

Given:  $W_A = 100$  (lb),  $W_B = 110$  (lb),  $\mu_k = 0.3$   
 $\theta = 20$  (deg), system is **released from rest**  
 $A$  moves **up the plane** and  $B$  moves **down**

Find:  $v_2$  the velocities of the two blocks  $\frac{1}{2}$  (sec) after release

Solution: (using the **principle of impulse & momentum**)



**Free body diagrams for motion up the plane**

Newton's Law:

$$A: \left[ + \nearrow \sum F_y = N - W_A \cos(\theta) = 0 \right] \Rightarrow \left[ f = \mu_k N = \mu_k W_A \cos(\theta) \right]$$

Impulse and Momentum:

$$A: \left[ L_{1x} + \sum (I_{1 \rightarrow 2})_x = L_{2x} \right] \text{ with } \left[ L_{1x} = \left( \frac{W_A}{g} \right) v_{1x} = 0 \right] \text{ (released from rest)}$$

$$\left[ L_{2x} = \left( \frac{W_A}{g} \right) v_2 \right] \text{ and } \left[ \sum (I_{1 \rightarrow 2})_x = (T - W_A \sin(\theta) - \mu_k W_A \cos(\theta)) \Delta t \right] \text{ (constant forces)}$$

$$\Rightarrow \left[ [T - W_A \sin(\theta) - \mu_k W_A \cos(\theta)] \Delta t = \left( \frac{W_A}{g} \right) v_2 \right] \quad (1)$$

$$B: \left[ L_{1x} + \sum (I_{1 \rightarrow 2})_x = L_{2x} \right] \text{ with } \left[ L_{1x} = \left( \frac{W_B}{g} \right) v_{1x} = 0 \right] \text{ (released from rest)}$$

$$\left[ L_{2x} = \left( \frac{W_B}{g} \right) v_2 \right] \text{ (same velocity as } A) \text{ and } \left[ \sum (I_{1 \rightarrow 2})_x = (W_B - T) \Delta t \right] \text{ (constant forces)}$$

$$\Rightarrow \left[ [W_B - T] \Delta t = \left( \frac{W_B}{g} \right) v_2 \right] \quad (2)$$

Adding equations (1) and (2) gives:

$$\left[ [W_B - W_A \sin(\theta) - \mu_k W_A \cos(\theta)] \Delta t = \left( \frac{W_A + W_B}{g} \right) v_2 \right]$$

$$\Rightarrow \left[ v_2 = \left( \frac{g \Delta t}{W_A + W_B} \right) [W_B - W_A \sin(\theta) - \mu_k W_A \cos(\theta)] = 3.64989 \approx 3.65 \text{ (ft/s)} \right]$$